

**October 30, 2023**

1. For a spinless particle, its wave function reads

$$\psi(x, y, z) = K(x + y + 2z)e^{-\alpha r}, \quad (1)$$

with  $K$  and  $\alpha$  being real constants. (a) What is the total angular momentum of the particle? (b) What is the expectation value of  $\hat{L}_z$ ? (c) If  $L_z$  is measured, what is the probability of obtaining  $L_x = \hbar$ ? (d) Calculate the probability density of finding the particle within the solid angle  $d\Omega$ .